# Lucien Hennecart

# Postdoctoral assistant researcher, University of Edinburgh

# CONTACT DETAILS

School of Mathematics	
James Clerk Maxwell Building Citizenship: French	
The University of Edinburgh	
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King's Buildings	
Edinburgh	
EH9 3FD	
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Webpage: https://www.maths.ed.ac.uk/~lhenneca/	
Office: 5420	
Employment	
The University of Edinburgh	Edinburgh
Postdoctoral Research Assistant. Supervisor: Ben Davison.	$September \ 2021 \ -$
Funded by an ERC Starting Grant (2021–2023) and then by the Royal Society (202	3-)
Education	
Université Paris-Saclay, Département de Mathématiques d'Orsay	Orsay
PhD in Mathematics. Advisor: Olivier Schiffmann	September 2018 – September 2021
Université Paris-Saclay, Département de Mathématiques d'Orsay	Orsay
M.Sc. in Fundamental Mathematics, with high honors	2017 - 2018
Agrégation de Mathématiques	
French diploma for higher education teaching, Rank: 5/305	July 2017
Université Rennes 1 and École Normale Supérieure de Rennes	Rennes and Bruz
First year of M.Sc. in Fundamental Mathematics, with high honors	2015 - 2016
Université Rennes 1 and École Normale Supérieure de Rennes	Rennes and Bruz
B.Sc. in Physics	2014 - 2016
Université Rennes 1 and École Normale Supérieure de Rennes	Rennes and Bruz
B.Sc. in Fundamental Mathematics, with high honors	2014 - 2015
Recruited as a trainee civil servant at the École normale supérieure de F	Rennes
Competitive exam following the "Classes préparatoires"	2014
Lycée Claude Fauriel	Saint-Étienne
Classes préparatoires aux grandes écoles	2012 - 2014
Two-year intensive program in preparation for the national "Grandes Écoles" comp	etitive exams

# Rewards

1. £1000 for Exceptional contribution to the School of Mathematics of the University of Edinburgh (2023)

# Publications

Perverse sheaves with nilpotent singular support on the stack of coherent sheaves on an elliptic curve, *Transformation Groups* (2022), 40 pages, arXiv:2101.03813

In this work, we give a new parametrization of the irreducible components of the global nilpotent cone for an elliptic curve. The methods employed can be used to prove an analogous result for weighted projective curves. This gives natural bases for the BPS Lie algebra of these curves, defined mathematically by Ben Davison. Moreover, this new parametrization allows us to prove that the characteristic cycle map on the category of spherical Eisenstein perverse sheaves is bijective. I will use these results in future works.

Microlocal characterization of Lusztig sheaves for affine and g-loops quivers, Representation Theory of the American Mathematical Society 26(02) (2022), 17 – 67, 51 pages, arXiv:2006.12780

In this work, we prove a conjecture of Lusztig for affine quivers: a simple perverse sheaf is in the Lusztig category if and only if its singular support is nilpotent. The motivation comes from an attempt to geometrize the constructible Hall algebra of a quiver in order to define a canonical basis, analogous to that of quantum groups.

Asymptotic behaviour of Kac polynomials, Experimental Mathematics (2021), 1–19, arXiv:2003.06929

We study some properties of Kac polynomials when we vary the set of edges of the quiver. The motivation comes from the search of the different functorial properties of the constructible Hall algebra of a quiver when the quiver varies.

Isotropic cuspidal functions in the Hall algebra of a quiver, Int. Math. Res. Not. IMRN, (15) (2019), 11514 – 11564, 51 pages, arXiv:1903.04378

The cuspidal functions of affine quivers are determined. These give a minimal system of generators of the constructible Hall algebra (Sevenhant and Van den Bergh proved furthermore that this algebra has the structure of a quantum group associated with a generalized Kac–Moody algebra). The goal is to determine canonical bases for Hall algebras. A byproduct of the main result is a new group of symmetries of the Hall algebra of an affine quiver.

# Preprints

Nonabelian Hodge isomorphisms for stacks and cohomological Hall algebras, preprint (2023), 37 pages, arXiv:2303.2307.09920

We complete the nonabelian Hodge theory triangle of isomorphisms for stacks between the Borel-Moore homologies of the Dolbeault, Betti and de Rham moduli stacks. We also explain how to realise the category of connections on a smooth projective curve as a subcategory of a 2-Calabi-Yau dg-category. This gives a cohomological Hall algebra structure on the Borel-Moore homology of the stack of connections on a smooth projective curve. In addition, we compare the cohomological Hall algebra structures at the relative and absolute levels for the three sides of NAHT: they all coincide. The comparison of the Borel-Moore homologies of the Dolbeault and Betti moduli stacks was previously considered by the author with Davison and Schlegel Mejia (without taking the cohomological Hall algebra structures into account). This paper completes this study and provides a CoHA enhancement of classical NAHT for curves.

(with Ben Davison and Sebastian Schlegel Mejia) **BPS algebras and generalised Kac-Moody algebras from 2-Calabi-Yau categories**, preprint (2023), 58 pages, arXiv:2303.12592

We define and study the BPS Lie algebra of arbitrary 2-Calabi-Yau categories, satisfying some assumptions (in particular, the stack of objects is an Artin stack having a good moduli space). This BPS Lie algebra is a generalised Kac-Moody algebra whose root datum is determined by the monoid of connected components of the good moduli space, the Euler form of the category and the intersection cohomology of the good moduli space. Consequences include (1) A proof in full generality of the positivity conjecture for absolutely cuspidal polynomials of Bozec-Schiffmann, a strengthening of the Kac positivity conjecture (2) A proof of the cohomological integrality conjecture for local K3 surfaces (3) A lowest weight vector description for the cohomology (in all degrees) of Nakajima quiver varieties.

(with Ben Davison and Sebastian Schlegel Mejia) BPS Lie algebras for totally negative 2-Calabi–Yau categories and nonabelian Hodge theory for stacks, preprint (2022), 76 pages, arXiv:2212.07668

We define the relative cohomological Hall algebra of any category whose stack of objects is an Artin stack with good moduli space of objects. When the category under consideration is 2-Calabi–Yau and totally negative, the BPS algebra is shown to be freely generated by the intersection cohomology of the good moduli space. This implies a nonabelian Hodge isomorphism for stacks and the positivity of cuspidal polynomials of quivers.

# On geometric realizations of the unipotent enveloping algebra of a quiver, preprint (2022), 29 pages, arXiv:2209.06552

We compare the different constructions of the positive part of the enveloping algebra of the Lie algebra associated to a quiver with possible loops,  $U(\mathfrak{n}^+)$ : constructible functions or perverse sheaves on the moduli stack of objects, functions on the seminilpotent stack and top-cohomological Hall algebra (CoHA) of the seminilpotent stack. As a byproduct, the top-CoHA of a quiver is shown to be isomorphic to  $U(\mathfrak{n}^+)$ .

(with Nikolai Perry) A Quiver Analogue of Higman's Conjecture, preprint (2022), 17 pages, arXiv:2208.07738

This paper has mainly been written by Nikolai Perry and is the outcome of an undergraduate summer research project at the University of Edinburgh. We define a new generalization of Higman's conjecture to quivers by considering the count of commuting pairs of radical endomorphisms of a projective representation. We prove compatibilities when performing operations on the quiver: reversing of arrows, splitting of a sink or a source,... The conjecture is proved in the first cases, in particular for acyclic quivers with at most three vertices.

# TALKS

Algebra and Geometry seminar, Liverpool	
BPS Lie algebras and action on the cohomology of Nakajima quiver varieties Algebra and Geometry seminar, Caen	23 November 2023
L'algèbre de Lie BPS	21 November 2023
Groups, Arithmetic and Algebraic Geometry Seminar (EPFL), Lausanne	
Nonabelian Hodge isomorphisms for cohomological Hall algebras	8 November 2023
GRIFT seminar, Edinburgh	
Instantons and AGT	17 October 2023
Algebra and Geometry seminar (HKUST), Hong-Kong	
Cohomological integrality for 2-Calabi-Yau categories	16 October 2023
Dublin Mathematics Colloquium, Geometry Seminar	
Cohomological integrality for 2-Calabi–Yau categories	28 September 2023
14th Ukraine algebra conference	
BPS algebras and generalised Kac–Moody Lie algebras from 2-Calabi–Yau categories	4 July 2023
VBAC webinar	
Nonabelian Hodge isomorphisms for stacks	5 June 2023
Séminaire SPACE, Université de Tours	
Comptage des représentations des algèbres lisses (On the count of representations of smooth of Université de Picardie Jules Verne Amiens	algebras) 10 March 2023
Comptage des représentations des clabbres lieses (On the count of representations of emoth.	alachrac) 0 March 2022
MFO Oberwolfach (5-day conference)	uigeoras) 9 march 2023
BPS Lie algebras for 2-Calabi-Yau categories and positivity of cuspidal polynomials	16 February 2023
Colloque tournant du GDR TLAG, Reims (3-day workshop)	
Positivité des polynômes cuspidaux (Positivity of cuspidal polynomials)	9 February 2023
Algebraic geometry seminar, McGill University, Montreal	
The BPS Lie algebra of 2-Calabi–Yau categories	27 January 2023
Séminaire du LACIM, Université du Québec à Montréal	
L'algèbre de Lie associée à un carquois (The Lie algebra associated to a quiver)	27 January 2023
Séminaire : Groupes, Représentations et Géométrie, University Paris-Cité	
Cohomological Hall algebras and stacky nonabelian Hodge theory	18 November 2022

MFO, 5-day conference	Oberwolfach
INVITED CONFERENCES	
Derived Categories, Moduli Spaces, and Counting Invariants Presentation of a poster "BPS algebras and generalised Kac–Moody algebras from 2-Ca	3 – 7 July 2023 labi–Yau categories"
Imperial College	London
COMMUNICATION	
Séminaire quantique de Strasbourg Cuspidal functions on the stack of representations of quivers	16 October 2019
Polynômes de Kac d'un carquois (Kac polynomials of quivers)	22 January 2020
PhD student seminar, Laboratoire de Mathématiques d'Orsay	
<b>Thematic trimester program on Representation theory, IHP, Seminar Youn</b> Microlocal characterization of Lusztig sheaves for extended Dynkin quivers	g researchers 19 February 2020
PhD students Day, Laboratoire de Mathématiques d'Orsay Microlocal characterization of Lusztig sheaves for affine quivers	15 September 2020
Réga Algèbres de Hall (Hall algebras)	7 April 2021
<b>Oberseminar Lie Theory Bochum</b> Cuspidal functions and Lusztig sheaves for affine quivers	17 Mai 2021
Séminaire de la Tortue, Genève The degree zero BPS Lie algebra of a curve	3 June 2021
Perverse sheaves with nilpotent singular support for curves and quivers	11 June 2021
Hodge seminar Polynomiality of the number of representations of the modular group Italian Representation Theory Seminar	7 October 2021
(Canonical) bases of the elliptic Hall algebra	25 October 2021
Séminaire d'algèbre	
Localization of equivariant cohomology Hodge Club Hall algebras	2 February 2022 29 October 2021
Perverse sheaves and hyperbolic localization SERG Reading Group, Edinburgh	17 March 2022
The top-CoHA of a curve Gdt Dualité symplectique, Orsay	21 March 2022
Equivariant (co)homology of affine Springer fibers EGRET Seminar, Edinburgh	29 March 2022
EGRET Seminar, Edinburgh Structure of cohomological Hall algebras Affine Springer fibers reading seminar, Edinburgh	17 October 2022
EGRET Seminar, Edinburgh	

MFO, 5-day conference	Oberwolfach
Representation Theory of Quivers and Finite-Dimensional Algebras	12 – 18 February 2023
Université de Reims, 3-day workshop	Reims
Colloque tournant du GDR TLAG	12 – 18 February 2023

# Scientific visits

EPFL	Lausanne
Visit of Dimitri Wyss and Tanguy Vernet to work on symmetrizable CoHAs	5 – 12 November 2023
Columbia University	New-York
Visit of Tudor Padurariu to discuss CoHAs	5 – 7 February 2023
McGill University	Montreal
Visit of Joel Kamnitzer to work on the relationship between canonical and semicanonical bases	25 – 27 January 2023
Université de Genève	Geneva
Visit of Nicolas Hemelsoet to work on factorizable sheaves	1 – 4 June 2021

## Undergraduate research experience

Laboratoire de Mathématiques d'Orsay	Orsay
Subject: Structure of the Hall algebra of a quiver. Supervisor: Olivier Schiffmann	February – August 2018
Institut Camille Jordan	Lyon
Subject: Topology of real algebraic varieties. Supervisor: Jean-Yves Welschinger	Mai – June 2016
Mathematisches Institut of Göttingen	Göttingen
Subject: Binary quadratic forms, the circle method and Waring's problem. Supervisor: Jörg Bri	dern June – July 2015

#### TEACHING EXPERIENCE

# 2023 - 2024 (University of Edinburgh)

• Submission of a proposal for a group project for fourth year students on Deligne categories.

#### 2022 - 2023 (University of Edinburgh)

• First semester: co-lecturer for the course "Introduction to Lie groups" for fifth year students (organized by Pavel Safronov)

#### 2021 - 2022 (University of Edinburgh)

- First semester: Reading course on Lie algebras for two fifth year students (organized with Iain Gordon). One-hour weekly meetings.
- Summer 2022: Supervisor of two summer research projects for third year undergraduate students
  - 1. Nikolai Perry: Around Higman's conjecture
  - 2. Yashh Kotecha: The algebra of the Gaudin system

#### 2020 – 2021 (Université Paris-Saclay)

- First semester: Exercise class "Algebra" for first year students, 36 hours
- Exercise class "Introduction to Lie algebras" in the master program AAG (Analyse, Arithmétique, Géométrie) (5-th year students), 12 hours

# 2019 – 2020 (Université Paris-Saclay)

- Mentoring of two Italian students laureate of an award of the FMJH (Fondation mathématique Jacques Hadamard) to attend the AAG (Analyse, Arithmétique, Géométrie) master program at Orsay
- First semester: Exercise class "Calculus" for first year students, 48 hours
- Second semester: Exercise class "Iterative methods in linear algebra" for third year students, 30 hours

#### 2018 – 2019 (Université Paris-Saclay)

- First semester: Exercise class "Calculus" for first year students, 16 hours
- Second semester: Exercise class "Linear algebra" for first year students, 48 hours

#### 2017 – 2018 (Lycée Blaise Pascal d'Orsay)

• Oral exams of mathematics for second year students, Lycée Blaise Pascal (Orsay). 2 hours per week, 50 hours altogether

# 17 – 21 April 2023

• Workshop on the Isle of Skye, "Vertex algebras and Hall algebras in enumerative geometry"

# 2021 -

• Organisation of the EGRET seminar in Edinburgh with Ben Davison and Sebastian Schlegel Mejia

# EXPERTISE

Reviewer for Zentralblatt, Mathscinet. Reviewer for several journals.

# LANGUAGES

French: Native speakerEnglish: Good skills. Toeic: 815/990 (2016); IELTS: Overall Band Score: 7.5 (2021)German: Level: C1 (Deutsches Sprachdiplom des Kultusministerkonferenz, 2012).

# Memberships

London Mathematical Society

#### MISCELLANEOUS

- I have been playing the Cello for 20 years. I have played in many different student orchestras over the years, participated to master-classes given by some of the famoust French or Italian cellists (Emmanuelle Bertrand, Xavier Gagnepain, Jean Deplace, Xavier Phillips, Claudio Pasceri). Cellist at the Edinburgh University Symphony Orchestra in 2021–2022 (fully auditioned orchestra). Cellist at the Edinburgh University Chamber Orchestra from 2022–2023 (fully auditioned orchestra). Cellist at the Edinburgh University Symphony Orchestra 2023–2024.
- 2. Member of the choir of the Edinburgh University Music Society (EUMS) from May 2023.
- 3. Member of the Edinburgh Young Walkers (EYW).